

Computational Modeling and Simulation of Earthquake Soil Structure Interaction Behavior of Nuclear Installations

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Outline

Introduction
Motivation
Uncertainties

Modeling and Simulation
Modeling and Simulation Examples
Probabilistic Inelastic Modeling

Summary

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Motivation

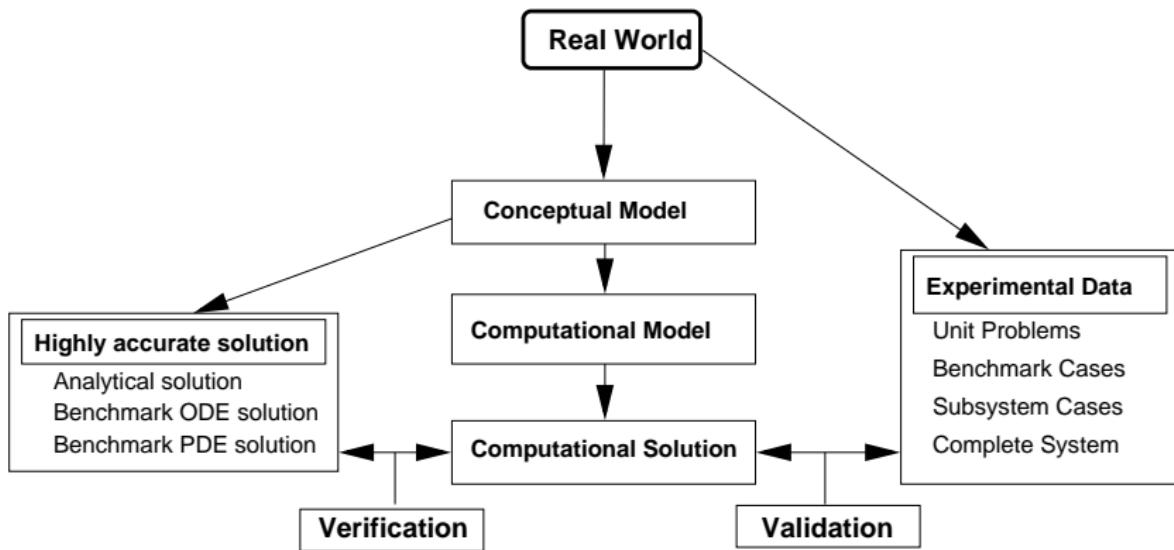
- ▶ Improve modeling and simulation for seismic behavior of Nuclear Installations
- ▶ Reduce modeling uncertainty
- ▶ Follow the flow, input and dissipation, of seismic energy,
- ▶ Practical system for modeling and simulation of Earthquakes, Soils, Structures and their Interaction (ESSI):

<http://real-essi.info/>

Predictive Capabilities

- ▶ Prediction under Uncertainty
- ▶ Verification: evidence that the model is solved correctly.
- ▶ Validation: evidence that the correct model is solved.
- ▶ Modeling and parametric uncertainties are always present
- ▶ Goal: Predict and Inform rather than (force) Fit
- ▶ Risk informed is not enough → full risk calculations for ESSI, analytical/numerical, accurate

Verification and Validation Details



Verification

The process of determining that a model implementation accurately represents the developer's conceptual description and specification.

- ▶ Identify and remove errors in computer coding
 - ▶ Numerical algorithm verification
 - ▶ Software quality assurance practice
- ▶ Quantification of the numerical errors in computed solution

Validation

The process of determining the degree to which a model is accurate representation of the real world from the perspective of the intended uses of the model.

- ▶ Tactical goal: Identification and minimization of uncertainties and errors in the computational model
- ▶ Strategic goal: Increase confidence in the quantitative predictive capability of the computational model

Types of Physical Experiments

► Traditional Experiments

- Improve the fundamental understanding of physics involved
- Improve the mathematical models for physical phenomena
- Assess component performance

► Validation Experiments

- Model validation experiments
- Designed and executed to quantitatively estimate mathematical model's ability to simulate well defined physical behavior
- The simulation tool, Real-ESSI, computational model, computational solution, is the customer

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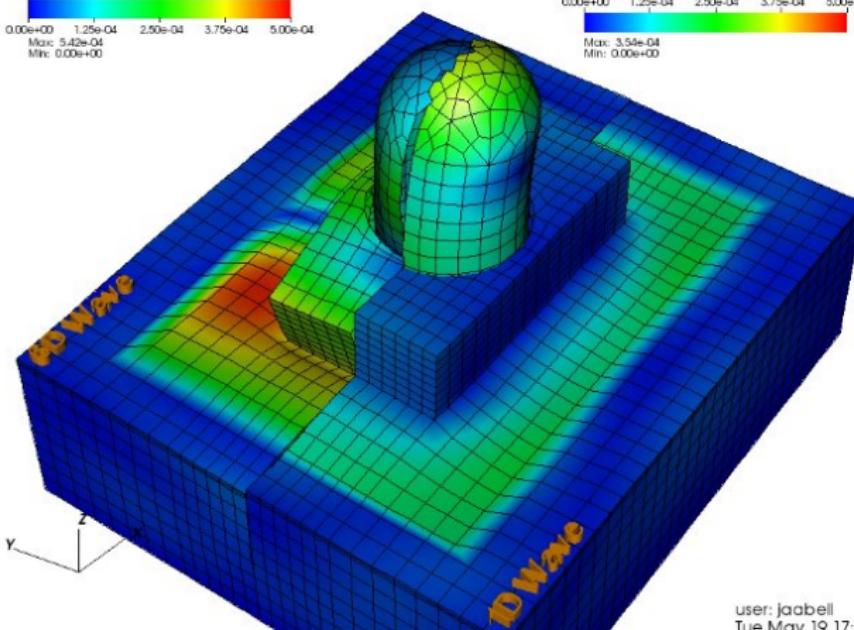
Uncertainties

- ▶ Modeling Uncertainty, from simplifying assumptions
 - ▶ Low, medium, high sophistication modeling and simulation
 - ▶ Sophistication level for confidence in analysis results
- ▶ Parametric Uncertainty, $M\ddot{u}_i + C\dot{u}_i + K^{ep}u_i = F(t)$
 - ▶ Propagation of uncertainty in M , C and K^{ep}
 - ▶ Propagation of uncertainty in loads, $F(t)$
 - ▶ Results are PDFs and CDFs for σ_{ij} , ϵ_{ij} , u_i , \dot{u}_i , \ddot{u}_i

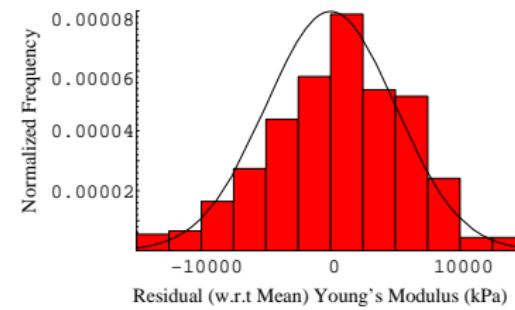
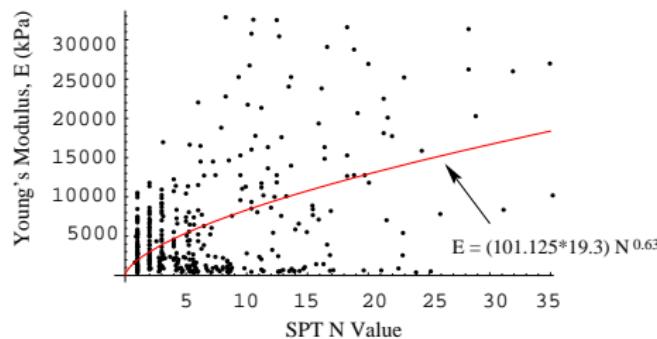
Modeling Uncertainty

- ▶ Simplified modeling: Features (important ?) are neglected (3C, 6C ground motions, inelasticity)
- ▶ Modeling Uncertainty: unrealistic and unnecessary modeling simplifications
- ▶ Modeling simplifications are justifiable if one or two level higher sophistication model shows that features being simplified out are not important

Modeling Uncertainty, 6C vs 1C Motions



Parametric Uncertainty: Soil Stiffness



cf. Phoon and Kulhawy (1999B)

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Modeling and Simulation Examples

Modeling and Simulation
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Energy Input and Dissipation

Energy input, static and dynamic forcing

Energy dissipation outside SSI domain:

- ▶ SSI system oscillation radiation
- ▶ Reflected wave radiation

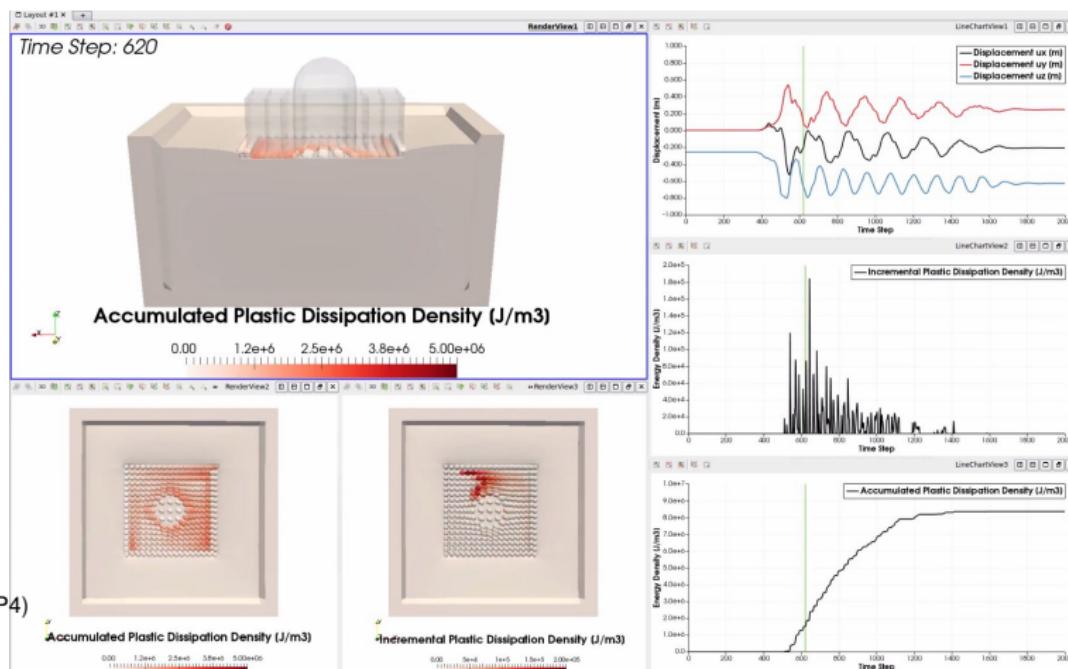
Energy dissipation/conversion inside SSI domain:

- ▶ Inelasticity of soil, contact zone, structure, foundation, dissipators
- ▶ Viscous coupling with internal/pore fluids, and external fluids

Numerical energy dissipation/production

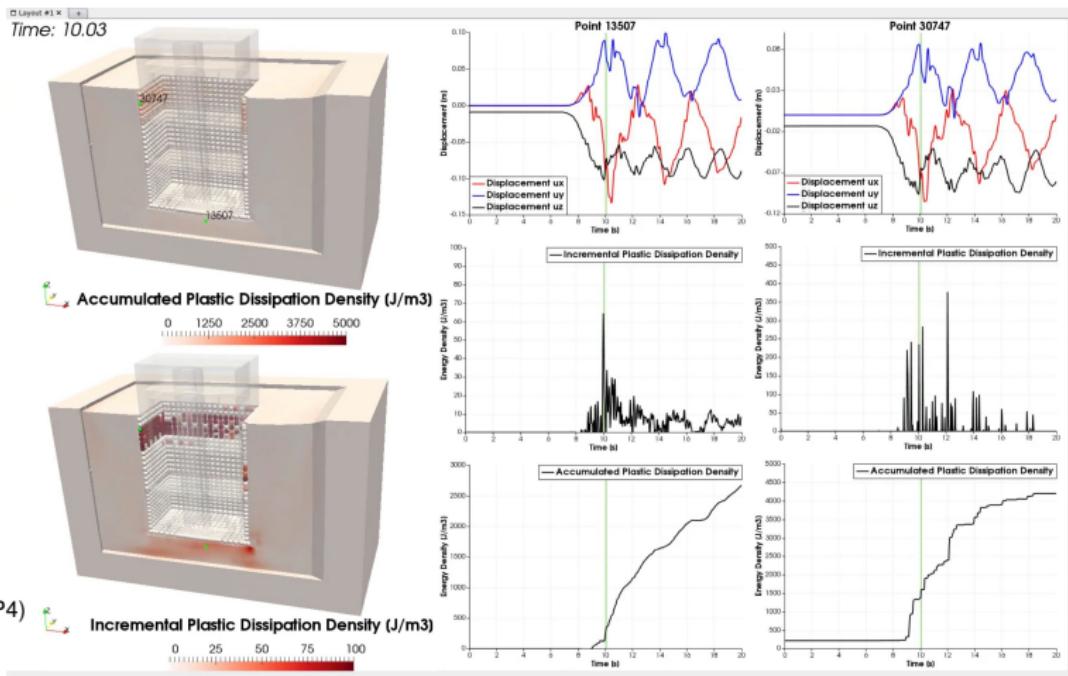
Modeling and Simulation Examples

Energy Dissipation in NPP Model



Modeling and Simulation Examples

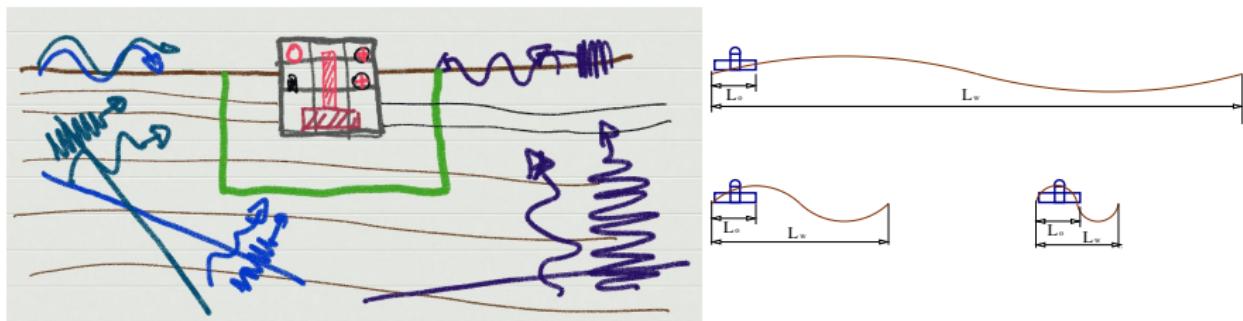
Energy Dissipation for an SMR Model



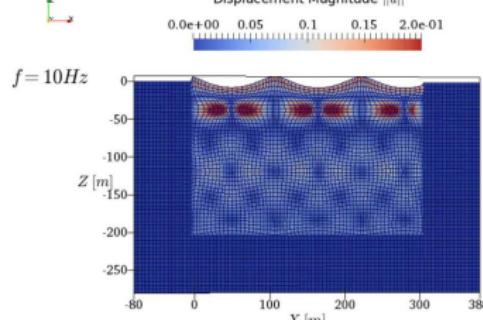
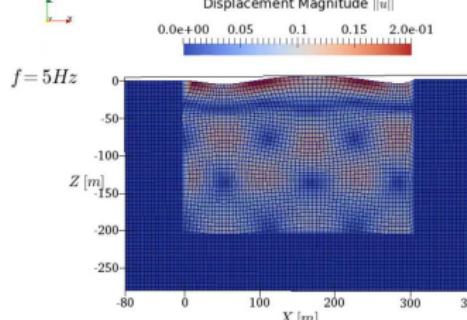
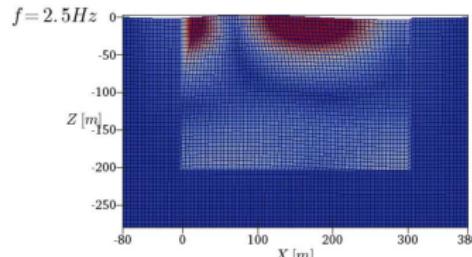
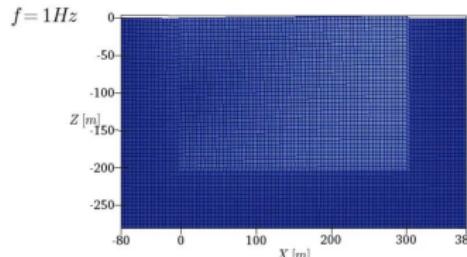
Modeling and Simulation Examples

Seismic Motions

- ▶ Variation in inclination, frequency, energy, duration...
- ▶ Deterministic and Probabilistic
- ▶ Stress test the soil-structure system



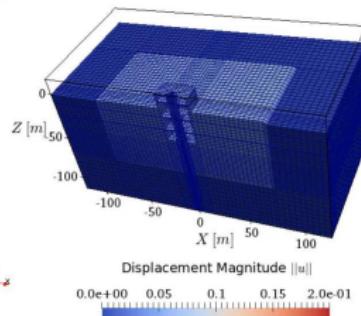
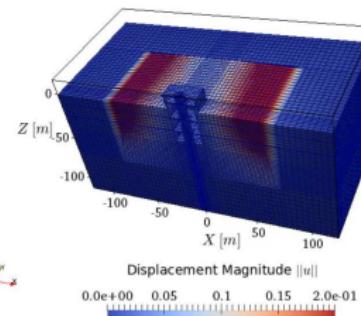
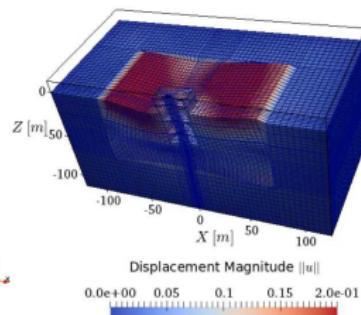
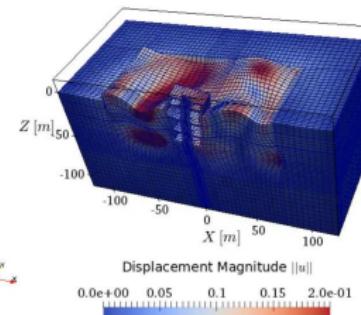
Modeling and Simulation Examples

Free Field, Variation in Input Frequency, $\theta = 60^\circ$ 

(MP4)



Modeling and Simulation Examples

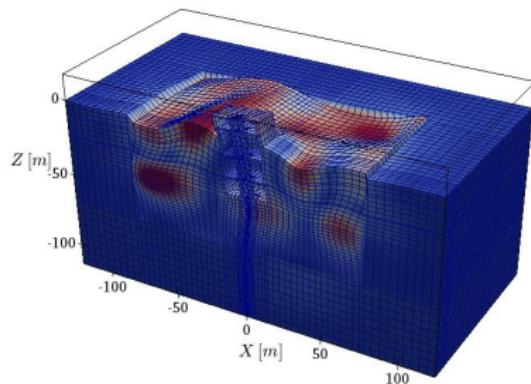
SMR ESSI, Variation in Input Frequency, $\theta = 60^\circ$ $f = 1\text{Hz}$  $f = 2.5\text{Hz}$  $f = 5\text{Hz}$  $f = 10\text{Hz}$ 

(MP4)

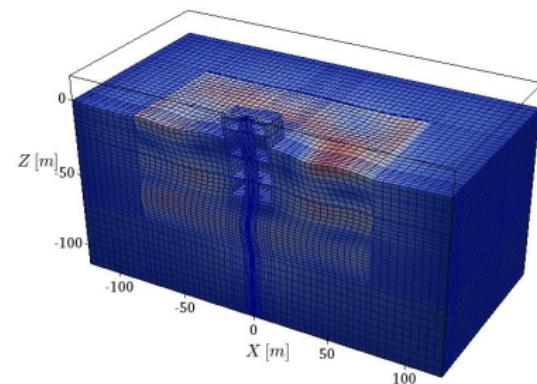
Modeling and Simulation Examples

SMR ESSI, 3C vs $3 \times 1C$

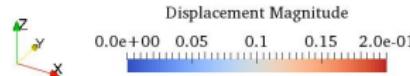
3C



$3 \times 1C$



(OGV)



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Uncertainty Propagation through Inelastic System

- ▶ Incremental el-pl constitutive equation

$$\Delta\sigma_{ij} = E_{ijkl}^{EP} \Delta\epsilon_{kl} = \left[E_{ijkl}^{el} - \frac{E_{ijmn}^{el} m_{mn} n_{pq} E_{pqkl}^{el}}{n_{rs} E_{rstu}^{el} m_{tu} - \xi_* h_*} \right] \Delta\epsilon_{kl}$$

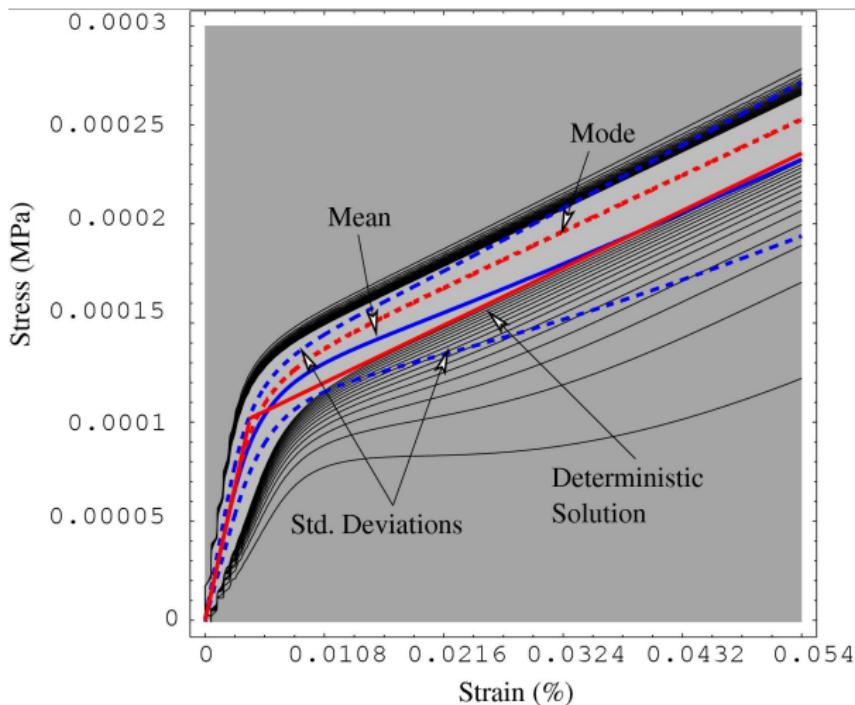
- ▶ Dynamic Finite Elements

$$M\ddot{u}_i + C\dot{u}_i + K^{ep}u_i = F(t)$$

- ▶ Material and load parameters are uncertain

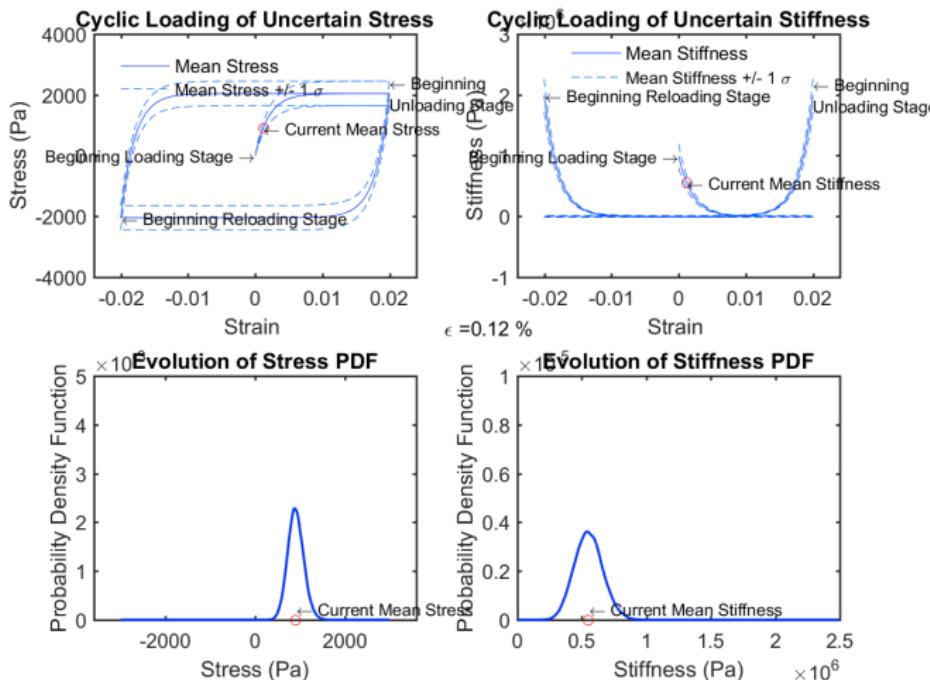
Probabilistic Inelastic Modeling

Probabilistic Elastic-Plastic Response



Probabilistic Inelastic Modeling

Probabilistic Elastic-Plastic Modeling



Stochastic Elastic-Plastic Finite Element Method

- ▶ Material uncertainty expanded into stochastic shape funcs.
- ▶ Loading uncertainty expanded into stochastic shape funcs.
- ▶ Displacement expanded into stochastic shape funcs.

$$\begin{bmatrix} \sum_{k=0}^{P_d} < \Phi_k \Psi_0 \Psi_0 > K^{(k)} & \dots & \sum_{k=0}^{P_d} < \Phi_k \Psi_P \Psi_0 > K^{(k)} \\ \sum_{k=0}^{P_d} < \Phi_k \Psi_0 \Psi_1 > K^{(k)} & \dots & \sum_{k=0}^{P_d} < \Phi_k \Psi_P \Psi_1 > K^{(k)} \\ \vdots & \vdots & \vdots \\ \sum_{k=0}^{P_d} < \Phi_k \Psi_0 \Psi_P > K^{(k)} & \dots & \sum_{k=0}^M < \Phi_k \Psi_P \Psi_P > K^{(k)} \end{bmatrix} \begin{bmatrix} \Delta u_{10} \\ \vdots \\ \Delta u_{N0} \\ \vdots \\ \Delta u_{1P_U} \\ \vdots \\ \Delta u_{NP_U} \end{bmatrix} = \begin{bmatrix} \sum_{i=0}^{P_f} f_i < \Psi_0 \zeta_i > \\ \sum_{i=0}^{P_f} f_i < \Psi_1 \zeta_i > \\ \sum_{i=0}^{P_f} f_i < \Psi_2 \zeta_i > \\ \vdots \\ \sum_{i=0}^{P_f} f_i < \Psi_{P_U} \zeta_i > \end{bmatrix}$$

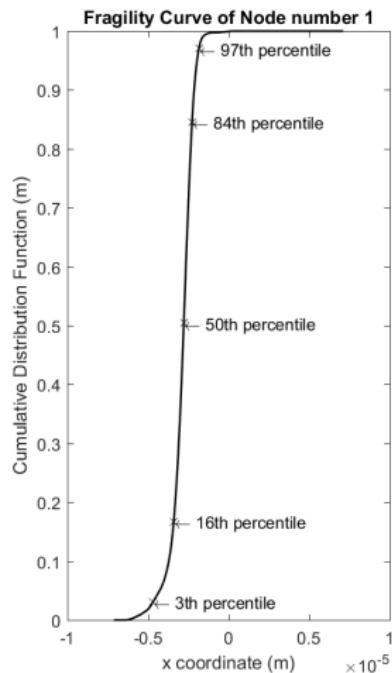
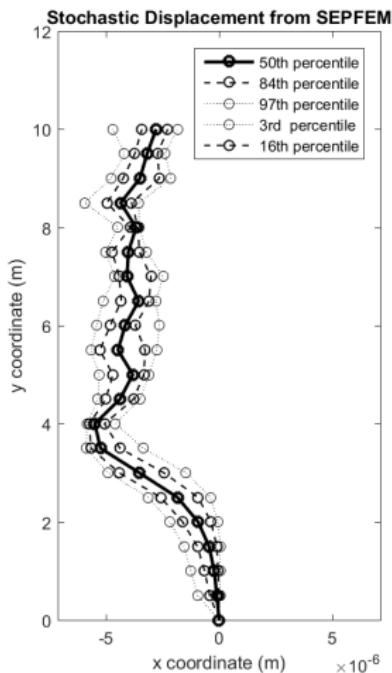
SEPFEM: System Size

- ▶ SEPFEM offers a complete solution (single step)
- ▶ It is NOT based on Monte Carlo approach
- ▶ System of equations does grow (!)

# KL terms material	# KL terms load	PC order displacement	Total # terms per DoF
4	4	10	43758
4	4	20	3 108 105
4	4	30	48 903 492
6	6	10	646 646
6	6	20	225 792 840
6	6	30	$1.1058 \cdot 10^{10}$
8	8	10	5 311 735
8	8	20	$7.3079 \cdot 10^9$
8	8	30	$9.9149 \cdot 10^{11}$
...

Probabilistic Inelastic Modeling

SEPFEM: Example in 1D



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- ▶ Numerical modeling to predict, rather than fit
- ▶ Education and Training is the key!
- ▶ Real-ESSI Simulator System:
<http://real-essi.info/>